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# Polarization Responses of a Solitary and Optically Injected Vertical Cavity Spin Laser

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**Abstract**—The polarisation properties of a quantum well spin – vertical cavity surface emitting laser (spin – VCSEL), both without injection and with variable polarisation optical injection, are investigated experimentally and compared with the spin flip model (SFM). Without injection, we demonstrate two distinct types of VCSEL-pump response depending on the signs of the linewidth enhancement factor, birefringence and dichroism: firstly where the pump and VCSEL have the same sign of the ellipticity, and secondly where the VCSEL ellipticity, accompanied by the linear polarisation, switches sign. We show that by controlling the injected power, ellipticity or linear angle, near circular polarisation can be obtained. These responses both give insight into the electro-optical injected spin-VCSEL system, and have practical implications for the use of spin VCSELs in unique applications exploiting the ellipticity degree of freedom.

**Index Terms**—VCSEL, spin, polarization, injection.

## I. INTRODUCTION

**S**PIN VCSELs – devices which utilise conservation of spin angular momentum in the electron-photon lasing processes – have been shown to possess a variety of unique characteristics. Properties such as threshold reduction [1], [2], spin amplification [3]–[5] polarisation control [5]–[8], and high frequency polarisation oscillations [9]–[12] have been demonstrated. These have raised awareness of the potential uses of spin lasers in future communications systems [13], [14]. Bistability and dynamics of the linearly polarised (LP) VCSEL modes with current [15], [16], temperature [17], or linear optical injection [18]–[27] have been investigated in recent years, due to their optical memory and logic applications. While the LP aspects have received considerable attention, the study of elliptic or circular injection into spin lasers, and the elliptic polarisation that

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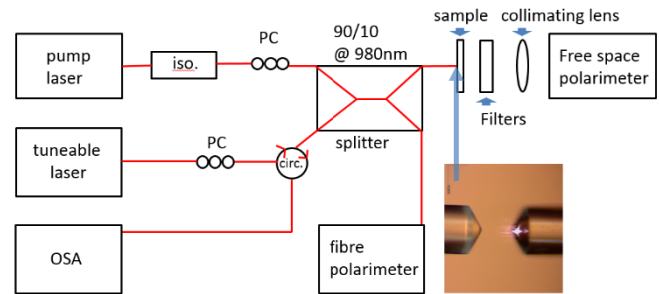


Fig. 1. Experimental set up. The splitter passed 59% of the 1300 nm light from the sample to the OSA, and from tuneable laser to sample.

results [28]–[31] is less well documented. The present contribution provides a link between these two sets of work. We conduct an in-depth investigation of injection of variable power, linear polarisation and elliptic polarisation into a spin VCSEL, both experimentally and theoretically. Through analysis of the electron spin, and the ellipticity of the injection and resultant VCSEL fields, we establish unique insight into the interaction of these parameters in both spin and non-spin lasers. Our investigations reveal unusual input-output ellipticity responses, and these are explained in terms of the spin VCSEL parameters via the SFM model. We demonstrate how these ellipticity responses can be altered and optimised, and finally we propose applications based on the ellipticity, to extend the current use of conventional VCSELs where the output is linearly polarised. Furthermore our investigation of the VCSEL polarisation is in accordance with a recent report [32] which highlights a common sign error for  $\alpha$  in the spin VCSEL literature. This paper is organised in six sections. In section II we describe our experimental set up. In section III we describe the polarisation terms and the spin flip model (SFM). The experimental and modelled results are presented in section IV, and these are discussed with regard to future work in section V. The conclusions are in section VI.

## II. EXPERIMENTAL SET UP

Our experimental set up is shown in figure 1. We use a dilute nitride quantum well (QW) 1300 nm VCSEL wafer grown at Tampere University of Technology, Finland. Our VCSEL design utilises epitaxial top and bottom DBR mirrors formed from AlAs/AlGaAs  $1/4$  wave layers (18 and 20.5 pairs respectively), and an active layer comprising 5 groups of GaInNAs QWs of 3 layers each, arranged at the antinodes of

the field profile. We have calculated the top and bottom mirror reflectivities as 99.6% and 99.8% respectively. The design is very similar to that described in [4], [7], [30], [31] except that it has an additional two pairs of top layers.

The  $8 \times 8$  mm cleaved wafer sample was bonded to a Si substrate and attached to a copper mount which was temperature controlled at  $17^\circ\text{C}$ . The VCSEL wafer was optically pumped through the top mirror using a packaged 980 nm grating stabilised laser using Corning HI1060© optical fibre via a splitter, and a polarisation controller (PC). This is a very similar experimental arrangement to that reported previously [4] except that instead of a cleaved fibre, here we used a high NA lens-ended fibre, enabling a minimum spot size of approximately 2.5  $\mu\text{m}$  FWHM. This enabled much better control of the photopumped area that defines the lasing region of the VCSEL. The lensed fibre was positioned by a dual manual/piezo-controlled stage. A splitter enabled a small proportion of the pump light in the fibre path to be directed to a fibre polarimeter to monitor the pump polarisation. The VCSEL output coupled back into the fibre along the return fibre path passed through the splitter and circulator into an optical spectrum analyser (OSA). A 1300 nm tunable laser (TL) of resolution 0.01 nm with a second PC was used to inject polarisation controlled light via the circulator and splitter. Reflection of the tunable laser from the sample surface, and VCSEL emission were both coupled into the fibre return path which allowed simultaneous observation of their spectra on the OSA. Thus the TL could be aligned to the resonance of the VCSEL lasing mode at 1300 nm. The output from the rear of the sample was filtered to remove the pump light and coupled into a free space polarimeter. This arrangement allowed separate measurement of the polarisations of the VCSEL emission and injected signal. When biased significantly below threshold, the injection polarisation could be measured directly, and this was verified to be the same without the VCSEL wafer in place, demonstrating that the single pass birefringence and dichroism of the wafer was small. With the VCSEL optically pumped above threshold, the resultant polarisation of the injected VCSEL could also be measured. Using this arrangement, the pump polarisation was recorded simultaneously with the native or injected VCSEL polarisation.

The VCSEL sample was optically pumped whilst observing the spectra at high resolution at different wafer positions, and a threshold pumping power of  $\sim 200$  mW was required for lasing, similar to figures published in [4], [7], [8]. The need for high pump power is largely due to the low absorption in the QW active region and single-pass pumping, as discussed in [4] and demonstrated in [33]. Once threshold had been identified, the VCSEL was biased at approximately 10% above the lasing threshold throughout subsequent measurements. A small bias above threshold has been shown to produce more useful polarisation responses [4]. Depending on the focus from the lensed-ended fibre, we observed distinct narrow and broad spectral peaks spaced between approximately 0.05 nm and 0.7 nm from each other. These were thought to be symptomatic of different spatial modes, and separate tests using a free space optical set up with an infra red camera confirmed this. By controlling the focusing, we isolated lasing in a short

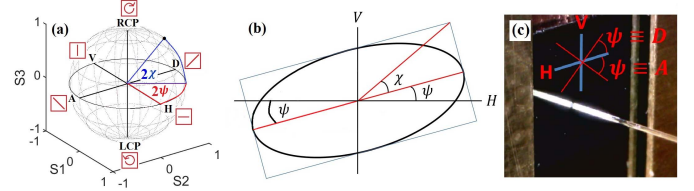


Fig. 2. Polarisation parameters. (a): Ellipticity ( $\chi$ ) and major axis angles ( $\psi$ ) on the Poincare sphere, with vertical (V), horizontal (H), diagonal (D) and anti-diagonal (A)  $\psi$  polarisations; (b) Polarization ellipse defining  $\psi$  and  $\chi$  (c) Wafer alignment with cleaved axis aligned to H, V (blue). The D, A example  $\psi$  values (red) show the degeneracy of  $\psi$  on the left and right sides of the diagram i.e. that  $\psi$  has a range of  $\pi$ .

wavelength, narrow spectral width peak, and found that the polarisation response of the VCSEL then gave results which were in good agreement with the spin flip model (SFM).

### III. POLARISATION TERMS AND THE SPIN FLIP MODEL

The polarisation is measured experimentally using the Stokes S1,2,3 parameters on the Poincare sphere. These are defined by the major axis angle of the polarisation ellipse  $\psi$ , and the ellipticity angle  $\chi$ , as shown in figure 2a,b and equations (1)-(4). Using (1) and (2),  $\psi$  can be derived with (5) using the 4-quadrant atan2 function, noting that both S3 and S2 are signed values. As the Stokes S1 and S2 parameters define  $\psi$ , we present the polarisation here via only the VCSEL major axis angle  $\psi_{VCSEL}$  and Stokes ellipticity  $S3_{VCSEL}$ . These are measured in terms of the pump polarisation ellipticity  $S3_{pump}$ , the injection ellipticity  $S3_{inj}$  and the injection angle  $\psi_{inj}$ .

$$S1 = \cos 2\chi \cos 2\psi \quad (1)$$

$$S2 = \cos 2\chi \sin 2\psi \quad (2)$$

$$S3 = \sin 2\chi \quad (3)$$

$$S1^2 + S2^2 + S3^2 = 1 \quad (4)$$

$$\psi = \frac{1}{2} \tan^{-1} \frac{S2}{S1} \quad (5)$$

We use the SFM with injection, originally presented in [34], without any consideration of misalignment between the axes of birefringence and dichroism (which has been investigated in e.g. [32], [35], [36]). The SFM in terms of the linearly polarised complex fields  $\tilde{E}_x$ ,  $\tilde{E}_y$ , is given in equations (6) to (9):

$$\begin{aligned} \frac{d\tilde{E}_x}{dt} = & \kappa (1 + i\alpha) \left[ (N - 1) \tilde{E}_x + im\tilde{E}_y \right] \\ & - (\gamma_a + i(\gamma_p + \Delta\omega)) \tilde{E}_x + \kappa_{inj} \tilde{E}_{inj,x} \end{aligned} \quad (6)$$

$$\begin{aligned} \frac{d\tilde{E}_y}{dt} = & \kappa (1 + i\alpha) \left[ (N - 1) \tilde{E}_y - im\tilde{E}_x \right] \\ & + (\gamma_a + i(\gamma_p - \Delta\omega)) \tilde{E}_y + \kappa_{inj} \tilde{E}_{inj,y} \end{aligned} \quad (7)$$

$$\begin{aligned} \frac{dN}{dt} = & -\gamma \left[ N \left( 1 + |\tilde{E}_x|^2 + |\tilde{E}_y|^2 \right) - (\eta_+ + \eta_-) \right] \\ & + im \left( \tilde{E}_y \tilde{E}_x^* - \tilde{E}_x \tilde{E}_y^* \right) \end{aligned} \quad (8)$$

$$\begin{aligned} \frac{dm}{dt} = & -\gamma_s m - \gamma \left[ m \left( |\tilde{E}_x|^2 + |\tilde{E}_y|^2 \right) - (\eta_+ - \eta_-) \right] \\ & + iN \left( \tilde{E}_y \tilde{E}_x^* - \tilde{E}_x \tilde{E}_y^* \right) \end{aligned} \quad (9)$$

$\tilde{E}_x$  and  $\tilde{E}_y$  are usually aligned to the horizontal ( $H$ ) and vertical ( $V$ ) axes, respectively.  $\kappa$  is the field decay rate,  $\gamma_a$  and  $\gamma_p$  the linear dichroism and birefringence,  $\gamma$  and  $\gamma_s$  the electron recombination and spin rates, and  $\alpha$  is the linewidth enhancement (Henry) parameter.  $\tilde{E}_{inj,x}$  and  $\tilde{E}_{inj,y}$  are the complex injection fields,  $\kappa_{inj}$  the injection rate and  $\Delta\omega$  the detuning between VCSEL and injection fields, which is here set to zero.  $\eta_+$ ,  $\eta_-$  are the spin up, down pumping parameters,  $N$  is the total (spin up and down) electron density and  $m$  is the difference in spin up, down electron populations. The hole relaxation rate is effectively instantaneous [7]. The pump ellipticity  $S3_{pump}$  is derived from  $\eta_+$ ,  $\eta_-$  using:

$$S3_{pump} = \frac{\eta_+ - \eta_-}{\eta_+ + \eta_-} \quad (10)$$

The generation of the Stokes parameters from the complex VCSEL fields  $\tilde{E}_x$ ,  $\tilde{E}_y$  is detailed in Appendix A1. The complex injection fields  $\tilde{E}_{inj,x}$ ,  $\tilde{E}_{inj,y}$  in (6) and (7) are generated from the defined  $S3_{inj}$ ,  $\psi_{inj}$  as per Appendix A2. We solve equations (6)-(9) in the time domain using a variable time-step Runge-Kutta method via the Matlab™ ode45 function. The time series were propagated for 80ns, with the polarisation averaged over the last 30ns where the time series converged to steady state solutions.

#### IV. EXPERIMENTAL AND MODELLED RESULTS

##### A. Solitary Spin VCSEL

The sample used here is the same design as that previously reported in [4], [7], [30], [31] but with the addition of two mirror pairs. In practice this did not result in any significant changes in measured output-pump characteristics; therefore we used values we calculated in [4] of  $\kappa$  ( $68.5 \text{ ns}^{-1}$ ) and the scaling above threshold of the pump rate  $\eta$  to the pump rate  $P/P_{th}$  (143%). The material parameters (derived from published experimental measurements of our material) are similarly unchanged, with  $\gamma = 1 \text{ ns}^{-1}$ ,  $\gamma_s = 64 \text{ ns}^{-1}$  and  $\alpha = -2$  (note sign). For this unprocessed wafer we anticipate small linear dichroism  $\gamma_a$  and birefringence  $\gamma_p$ . To begin with we performed detailed experimental characterisation of the elliptic and linear polarisation of the solitary photopumped sample i.e.  $\psi_{VCSEL}$ ,  $S3_{VCSEL}$  in terms of  $S3_{pump}$  (figures 3a-d). We then fitted these measurements to the SFM through variation of  $\gamma_a$  and  $\gamma_p$ , deducing values of  $\gamma_a = 0.1 \text{ ns}^{-1}$  and  $\gamma_p = 2 \text{ ns}^{-1}$ . Next we note that care needs to be taken over the sign of the  $\alpha$  parameter as it appears in the SFM equations, which has been highlighted recently [32]. In a similar vein we also consider the influence of the signs of the birefringence and dichroism. We tested this with examples of two distinct types of experimental polarisation response that are found in the SFM without injection. The first type of response is plotted in figure 3e and characterised by an S-shaped VCSEL-pump ellipticity curve, where  $S3_{VCSEL}$  and  $S3_{pump}$  are of the same sign, and there is a small rotation i.e. change in  $\psi_{VCSEL}$  (figure 3f). This type relates to responses and wafer samples in [4], [7], and is modelled with values of  $\gamma_a$  and  $\gamma_p$ , of  $0.05 \text{ ns}^{-1}$  and  $-0.35 \text{ ns}^{-1}$  respectively. This type of response is commonly found in the spin VCSEL

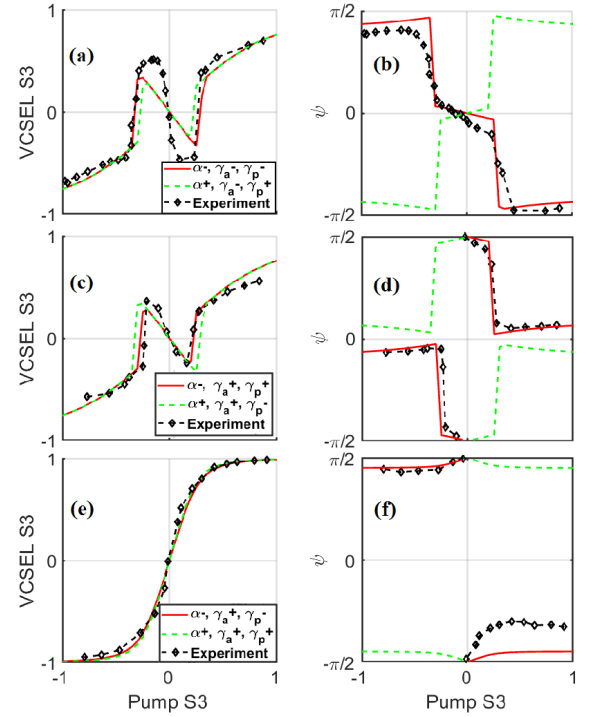


Fig. 3. Experimental and SFM polarisation responses with signed values of  $\alpha$ ,  $\gamma_a$  and  $\gamma_p$ : (a), (b) Switching response with greater gain in H axis ( $\gamma_a^-$ ); (c), (d) Switching response with greater gain in the V axis ( $\gamma_a^+$ ); (e), (f) S-shaped response with  $\gamma_a^+$ . The remaining two of eight SFM sign combinations (from  $\alpha^{+/-}$ ,  $\gamma_a^{+/-}$  and  $\gamma_p^{+/-}$ ) which give an S-shaped response with  $\gamma_a^-$  are not shown, as a suitable experimental example was not available.

literature [3]–[8] and usually characterises spin amplification of the pump. A second type, found in the sample used in this work is characterised by a switch in  $S3_{VCSEL}$  to the opposite sign of  $S3_{pump}$  (figure 3a,c), accompanied by a large rotation of  $\psi_{VCSEL}$  of nearly  $\pi/2$  at each switching point (figure 3b,d). This type of response has been investigated in [37] and is shown to be due to switching between two stable solutions of the SFM equations, although the large rotation of  $\psi_{VCSEL}$  with  $S3_{pump}$  does not appear to have been reported previously.

Figure 3 shows that with negative  $\alpha$  in the SFM, the switching response occurs when the dichroism  $\gamma_a$  and birefringence  $\gamma_p$  are of the same sign (red lines, figure 3a,c), and the S-shaped response occurs when they are of opposite sign (red lines figure 3e). Conversely for positive  $\alpha$ , the switching response occurs when  $\gamma_a$  and  $\gamma_p$  are of opposite signs (green lines, figure 3a,c) and the S-shaped response occurs when they are of the same sign (green line figure 3e). This holds for all except very small values of  $\gamma_a$  and  $\gamma_p$ , hence care is needed in that circumstance. Changing only the signs of  $\alpha$  (and  $\gamma_a$ ,  $\gamma_p$ ) to maintain the type of polarisation response is seen to change the  $S3_{VCSEL}$  values only marginally (figure 3a,c,e) however the SFM polarisation paths  $\psi_{VCSEL}(S3_{pump})$  change dramatically (figures 3b,d,f), revealing a match in the sign of  $\psi_{VCSEL}$  between the experiment (black lines figure 3b,d,f) and SFM only when  $\alpha$  is negative (red lines). Moreover for other sign combinations, or variation of these parameters,  $\psi_{VCSEL}$  and  $S3_{VCSEL}$  are not well reproduced. When focussing solely



on the VCSEL ellipticity, which is common for spin lasers, the sign of  $\alpha$  in the SFM is not critical. However this study of  $\psi_{VCSEL}$  reveals  $\alpha$  must be negative, and thus, care must be taken in formulism of the SFM [32], [34], to ensure  $\alpha$  appears appropriately signed.

The two experimental examples of the switching responses in figure 3a,b and 3c,d were achieved by rotating the wafer planar axes by 90 degrees. There is a noticeable difference in the  $S3_{VCSEL}$  paths between these two results, with figure 3c,d better reproduced by the SFM, but this is representative only of the small variation in ellipticity responses observed in this wafer and unrelated to the axis orientation. Noting the signs in equations (6) and (7), positive  $\gamma_a$  and  $\gamma_p$  give higher gain and frequency for the  $y$  polarisation and lower values in the  $x$  polarisation. As the physical H,V axes have been switched between these two orientations, the signs of both  $\gamma_a$  and  $\gamma_p$  are correspondingly reversed in the SFM. Despite the flexibility that the SFM sign convention gives for the *absolute* signs of  $\gamma_a$  and  $\gamma_p$  depending on orientation, the *relative* signs of  $\gamma_a$  and  $\gamma_p$  are physically significant, as the spin VCSEL system will display very different behaviour with higher gain and frequency in the same axis than in different axes, as shown above. Both signed [35] and absolute [38] frequency differences between the orthogonal [110] and  $[\bar{1}\bar{1}0]$  crystallographic axes for QW spin-VCSELs have been recently published. In [34] both negative and positive frequency splitting between [110] and  $[\bar{1}\bar{1}0]$  was seen, and in each case the gain splitting was of opposite sign to the frequency splitting. However the existence of the switching response in figure 3 and [37] indicate that (with a negative  $\alpha$ ) the gain and frequency splitting (which broadly define  $\gamma_p$  and  $\gamma_a$ ) can have the same sign.

### B. Spin VCSEL With Optical Injection

We applied optical injection to our wafer and examined the VCSEL polarisation  $S3_{VCSEL}$ ,  $\psi_{VCSEL}$  as a function of pump and injection ellipticity  $S3_{pump}$ ,  $S3_{inj}$  and injection angle  $\psi_{inj}$ . Hereon we adopt a common set of SFM parameters  $\gamma_a = +/ - 0.1 \text{ ns}^{-1}$ ,  $\gamma_p = +/ - 2 \text{ ns}^{-1}$  and  $\alpha = -2$ , with any variation being noted. The  $\gamma_{a,p}$  signs (from wafer orientation) are also noted. Although the injection power was 2 mW, the optical coupling efficiency into the VCSEL mode is expected to be small, and will be sensitive to the fibre position. We found that an injection rate  $\kappa_{inj}$  between  $0.015\kappa$  and  $0.04\kappa$  produced a good SFM match to the range of experimental results (noted for each experiment below). This range of  $\kappa_{inj}$  values is an order of magnitude lower than those in [29]–[31], which used a different experimental set up, including higher pump rate and injection power. In figure 4 the VCSEL polarisation was recorded with swept  $S3_{pump}$  as in figure 3, but with fixed  $S3_{inj}$  of zero (figure 4(a),(c)) and  $S3_{inj} = \sqrt{1/2}$  (figure 4(b),(d)), together with four equally spaced angles of  $\psi_{inj}$  i.e. H,V, diagonal (D) and antidiagonal (A). The  $\gamma_{a,p}^+$  orientation was used. The experimental result for  $S3_{inj} = 0$  shows the switching has been suppressed and the VCSEL ellipticity is increased for  $\psi_{inj} \equiv A$  and reduced for  $\psi_{inj} \equiv D$  (figure 4a). It is also increased somewhat for  $\psi_{inj} \equiv V$  and decreased somewhat for  $\psi_{inj} \equiv H$ . The same trend is found

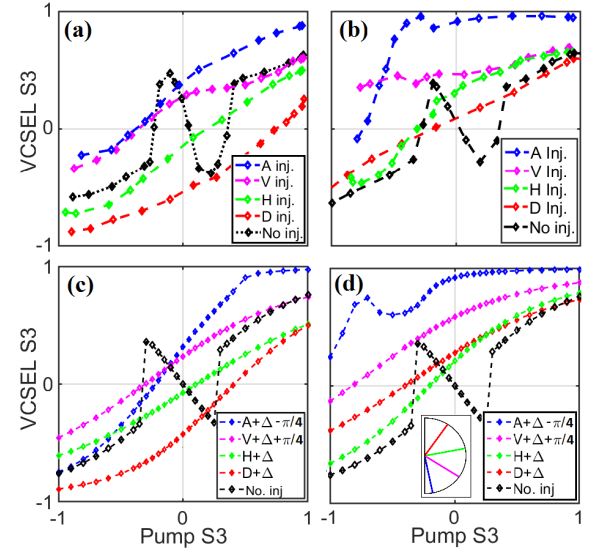


Fig. 4. VCSEL Stokes  $S3$  parameter versus pump  $S3$  with injection angles horizontal ( $H$ ,  $\psi_{inj} = 0$ ), vertical ( $V$ ,  $\psi_{inj} = \pi/2$ ), diagonal ( $D$ ,  $\psi_{inj} = \pi/4$ ) and antidiagonal ( $A$ ,  $\psi_{inj} = -\pi/4$ ) (a), (b) experiment and (c), (d) SFM.  $S3_{inj}$  is zero (a), (c) and  $\sqrt{1/2}$  (b) (d). The  $\gamma_{a,p}^+$  orientation was used. The SFM  $\Delta$  parameter is a rotation of  $\pi/16$ . The SFM injection rate was  $\kappa_{inj}/\kappa = 0.025$ .

for  $S3_{inj} = \sqrt{1/2}$  in figure 4b. This indicates that there is an angle between  $A$  and  $V$  that maximises the ellipticity, and an angle between  $D$  and  $H$  that minimises it.

In figure 4b it is seen that a VCSEL ellipticity close to  $+1$  is found for  $A$  injection, which is above the injection ellipticity of  $0.71$ , and this is achieved even for zero or negative  $S3_{pump}$ . This constitutes spin amplification of the injection. In figure 4a, a negative or positive  $S3_{VCSEL}$  is produced with  $S3_{inj} = 0$ , even for linear pumping, which constitutes spin generation (in this isolated system). Comparing the experiment to the SFM, we find that this unusual behaviour can be reproduced well. Figures 4c,d show a reasonable match with again four equally spaced angles  $\psi_{inj}$ , although the closest results to the experiment were found with an additional rotation  $\Delta$  of  $\pi/16$  from HVAD, with the  $A$  and  $V$  angles switched, as per figure 4c,d legend and 4d inset.

The response of  $S3_{VCSEL}$  to injection ellipticity,  $\psi_{inj}$  in figure 4 was investigated further by taking a finer step of  $\psi_{inj}$ , with linear pump and injection ellipticity, shown in figure 5. The experimental response (figure 5a) in the same  $\gamma_{a,p}^+$  orientation as figure 4 shows a positive peak in  $S3_{VCSEL}$  for  $\psi_{inj}$  between  $V$  and  $A$ , and a negative peak in  $S3_{VCSEL}$  for  $\psi_{inj}$  between  $V$  and  $D$ . This accords with the  $S3_{VCSEL}(\psi_{inj})$  values in figure 4. The equivalent response in the  $\gamma_{a,p}^-$  orientation (“orientation 2”) is also shown, together with the modelled responses in figure 5b. The angle  $\psi_{inj}$  that maximises  $|S3_{VCSEL}|$  is closer to the higher frequency axis -  $V$  for the  $\gamma_{a,p}^+$  orientation, and  $H$  for the  $\gamma_{a,p}^-$  orientation. This peak in  $|S3_{VCSEL}|$  for linear pumping and linear injection has been demonstrated before in the SFM in [29] figure 16c. Only a negative  $S3_{VCSEL}$  peak is shown in [29], as the angular parameter  $\theta_p$  is used there,

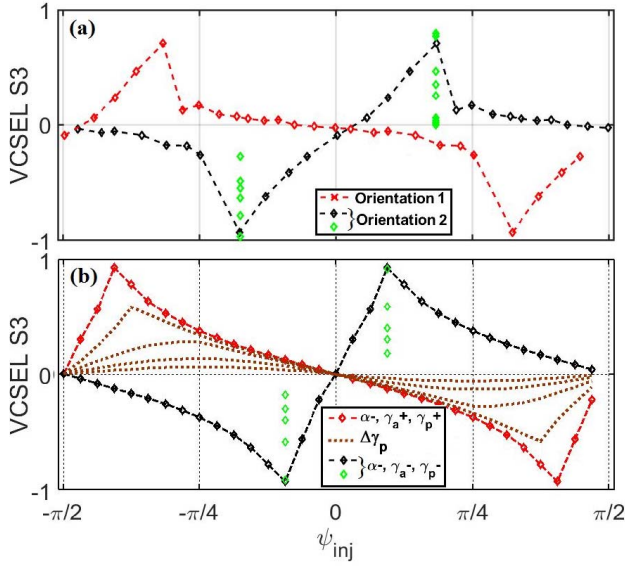


Fig. 5. VCSEL S3 versus  $\psi_{inj}$  for the case of linear pump and injection ellipticity; (a) Experimental  $S3_{VCSEL}$  (b) SFM  $S3_{VCSEL}$ .  $\kappa_{inj}$  is  $0.015 \times \kappa$  (red, black and brown lines) and  $0.015, 0.02, 0.03, 0.04, 0.06 \times \kappa$  with decreasing S3 magnitude (green markers).  $\gamma_p$  varies (four brown dotted lines) as 0.1, 0.5, 1 and  $1.5 \text{ ns}^{-1}$  with increasing S3 magnitude.

which has half the polarisation range of  $\psi$ . The ellipticity peak is dependent on a particular ratio of injection rate to pump rate, or correspondingly injection field to VCSEL field. This is demonstrated in figure 5a from variation of pump power (green markers), giving an  $S3_{VCSEL}$  range from nearly zero to  $\pm 1$ . This could also be achieved by variation of the injection power in the experiment. A similar range is shown using the SFM figure 5b from variation of  $\kappa_{inj}/\kappa$ . By testing the SFM response for the sign of  $\alpha$  we confirm agreement with the experiment is only for negative values.

To examine in more detail the  $S3_{VCSEL}(\psi_{inj})$  behaviour with the SFM, we firstly note from equation (A3) of Appendix A1 that S3 is written in terms of the phase difference  $\phi$  and absolute field magnitudes as (11).

$$S3 = -2|\tilde{E}_x||\tilde{E}_y|\sin\phi / (|\tilde{E}_x|^2 + |\tilde{E}_y|^2) \quad (11)$$

For the case  $S3_{inj} = 0$  here,  $|\tilde{E}_{inj,x}| = \cos(\psi_{inj})$ ,  $|\tilde{E}_{inj,y}| = \sin(\psi_{inj})$ . We find that for small  $\gamma_a, \gamma_p$  the injection  $x, y$  field magnitudes fully control the VCSEL  $x, y$  field magnitudes, except with very small injection magnitudes. Therefore  $|\tilde{E}_x| \propto \cos(\psi_{inj})$ ,  $|\tilde{E}_y| \propto \sin(\psi_{inj})$  and if the phase remains fixed, using this in (11) we find that S3 is sinusoidal with  $\psi_{inj}$  as (12).

$$S3 \propto \pm \cos(\psi_{inj}) \sin(\psi_{inj}) \propto \pm \sin(2\psi_{inj}) \quad (12)$$

This is found in the SFM with small  $\gamma_p$  and  $\gamma_a$ , as shown by the lowest magnitude S3 brown line in figure 5b. Under these conditions the VCSEL is acting like a waveplate, viz. fixing the  $x, y$  phase difference, whilst the injection angle controls the relative  $x, y$  magnitudes and subsequent S3. As the fields are positive and real in (11),  $0 \leq \psi_{VCSEL} \leq \pi/2$  so the sign choice from the phase gives the positive and negative S3 range. This is equivalent to removing the sign choice and accounting

for the phase in  $\psi_{inj}$ , giving  $-\pi/2 \leq \psi_{inj} \leq \pi/2$ . For these SFM parameters, the phase is fixed close to 0,  $\pm \pi$  giving a small  $|S3|$ , but we find for small  $\eta$  and  $\kappa_{inj}$  it approaches  $\pm \pi/2$ , giving S3 approaching LCP/RCP. With the standard  $\eta$  and  $\kappa_{inj}$ , but increasing  $\gamma_p$  to the expected physical level of  $2 \text{ ns}^{-1}$ , we find the phase starts to vary, and also  $|\tilde{E}_x|, |\tilde{E}_y|$  are no longer purely sinusoidal with  $\psi_{inj}$ . Consequently the  $|S3|$  peak becomes larger and skews towards the higher frequency axis (brown dotted lines figure 5b). This skewing, together with the S3 dependence on injection/pump rate, can be understood from the steady-state SFM with circular solutions. Substituting the LCP conditions  $\tilde{E}_y = i\tilde{E}_x$  in (6) and  $\tilde{E}_x = -i\tilde{E}_y$  in (7), assuming negligible  $\gamma_a$  gives

$$\kappa(1+i\alpha)[N-1-m]\tilde{E}_x - i\gamma_p\tilde{E}_x = -\kappa_{inj}\tilde{E}_{inj,x} \quad (13)$$

$$\kappa(1+i\alpha)[N-1-m]\tilde{E}_y + i\gamma_p\tilde{E}_y = -\kappa_{inj}\tilde{E}_{inj,y}. \quad (14)$$

Equations (13) and (14) define the injection magnitude for this circular solution as:

$$\kappa_{inj} = -[\kappa(1+i\alpha)(N-1-m) - i\gamma_p] \frac{\tilde{E}_x}{\tilde{E}_{inj,x}} \quad (15)$$

$$\kappa_{inj} = -[\kappa(1+i\alpha)(N-1-m) + i\gamma_p] \frac{\tilde{E}_y}{\tilde{E}_{inj,y}} \quad (16)$$

Variation from this optimum rate means the circular solutions do not hold, and the ellipticity will reduce as seen by the results in green, figure 5. Finally, from the ratio of (13) and (14):

$$\frac{\tilde{E}_{inj,x}}{\tilde{E}_{inj,y}} = \frac{[\kappa(1+i\alpha)(N-1-m) - i\gamma_p]\tilde{E}_x}{[\kappa(1+i\alpha)(N-1-m) + i\gamma_p]\tilde{E}_y} \quad (17)$$

Equation (17) shows that as  $\gamma_p \rightarrow 0$ , the injection ratio  $\tilde{E}_{inj,x}/\tilde{E}_{inj,y}$  approaches unity for this circular polarisation condition of  $|\tilde{E}_x| = |\tilde{E}_y|$  i.e.  $\psi_{inj} = \pm \pi/4$ . For finite positive (negative)  $\gamma_p$ ,  $\tilde{E}_{inj,x}/\tilde{E}_{inj,y}$  reduces (increases) from unity, and the S3 peak in  $\psi$  moves towards the higher frequency axis in both cases. This simplified analysis indicates in terms of the  $\tilde{E}_x, \tilde{E}_y$  magnitudes indicates why the S3 peak moves towards the higher frequency axis, but further analysis would be required to understand the phase variation (noted above) which also controls this process.

With the effect of  $\psi_{inj}$  now determined, the dependence of the  $S3_{VCSEL}(\psi_{inj})$  relation on the spin relaxation rate  $\gamma_s$  is now investigated in the SFM with finite  $S3_{inj}, S3_{pump}$  of 0.38, and with two values of  $\gamma_p$  (figure 6). In figure 6a,  $S3_{VCSEL}$  increases with reducing  $\gamma_s$ , as the resultant increasing spin polarisation exerts greater control of the resultant ellipticity. However the ellipticity peak close to the RCP axis occurs almost independently of  $\gamma_s$ . Indeed, the SFM results in figure 5b and [29] for linear pumping are found to change negligibly if  $\gamma_s = \infty$ , as there is no differential electron spin  $\uparrow, \downarrow$  excitation from the pump in that case. In figure 6b, the same results are shown, but with reduced birefringence. The VCSEL ellipticity is now principally controlled by the pump and injection ellipticity and shows reduced dependence on  $\psi_{inj}$ . With smaller  $\gamma_p$  (or  $\alpha$ ) we also observe that any

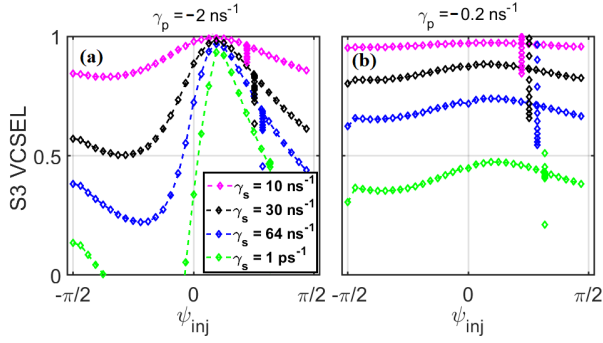


Fig. 6. SFM  $S3_{VCSEL}$  with  $\psi_{inj}$  for, with finite  $S3_{inj}$ ,  $S3_{pump}$  of 0.38, and  $\kappa_{inj} = 0.015$ . The  $\gamma_{a,p^-}$  orientation is used (c.f. figure 5 black line) (a)  $\gamma_p = -2 \text{ ns}^{-1}$  (b)  $\gamma_p = -0.2 \text{ ns}^{-1}$ . The vertical markers show variation of  $\kappa_{inj}$  from 0.015 to  $0.06 \times \kappa$  as per figure 5.

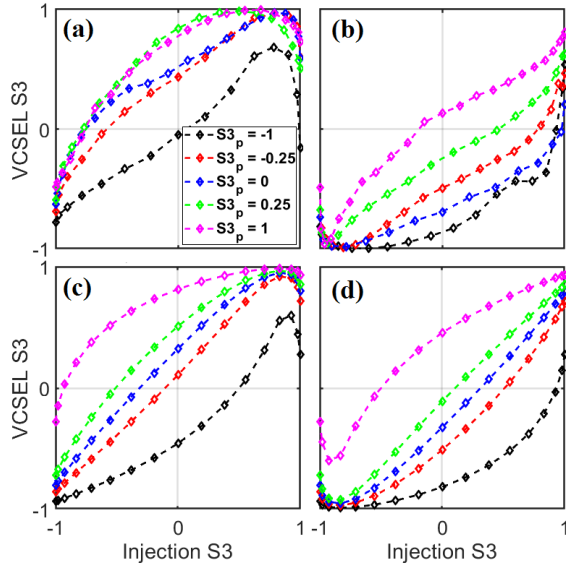


Fig. 7. VCSEL S3 versus injection S3 (a) Experimental,  $\psi_{inj} \equiv A$ , (b) Experimental,  $\psi_{inj} \equiv D$ , (c) SFM,  $\psi_{inj} = A - 3/32\pi$ , (d) SFM,  $\psi_{inj} = D + 3/32\pi$ .  $\gamma_p$  is  $+2 \text{ ns}^{-1}$ . The SFM injection rate was  $\kappa_{inj}/\kappa = 0.04$ . The legend in 7a applies to plots (a)-(d), with the  $S3_p$  denoting  $S3_{pump}$ .

oscillation in time between the  $H, V$  fields is more strongly damped. This accords with the polarisation oscillations that are observed for high birefringence in some cases [9]–[11]. For low  $\gamma_s$ , where the differential spin populations become much more significant and therefore control the ellipticity, the  $S3_{VCSEL}(\psi_{inj})$  relation is almost flat.

We now focus on the VCSEL output, vs. injected input ellipticity transfer characteristics of this system. Figure 7a-d shows the  $S3_{VCSEL}(S3_{inj})$  relation in the experiment and that from the SFM with  $\gamma_{a,p^+}$  signs, for  $\psi_{inj} \equiv A$  and  $\psi_{inj} \equiv D$ , giving a generally positive and negative  $S3_{VCSEL}$  respectively. Note the symmetry of these results, which follows from the negligible (zero) circular anisotropies in the experiment (SFM). The pump is varied from LCP to RCP ( $S3_{pump} = -1$  to  $+1$ ). A good general fit of model to experiment is obtained by using a small shift of  $\psi_{inj} = A - 3/32\pi$  and  $\psi_{inj} = D + 3/32\pi$  in the SFM. This is consistent with the small

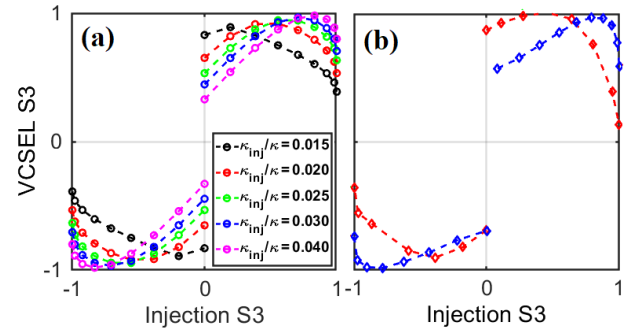


Fig. 8. VCSEL S3 versus injection S3 with linear pumping and varying injection magnitude (a) SFM ( $\gamma_p = 2 \text{ ns}^{-1}$ ) (b) experiment, with higher (blue) and lower (red) injection coupling.

$\psi_{inj}$  shift in figure 4, and the ellipticity peaks in figure 5, which are somewhat closer ( $\sim 3/32\pi$ ) to the  $V$  axis in the SFM than in the experiment. These small differences in experimental to modelled results can be expected considering the relative simplicity of the model. The  $S3_{VCSEL}(S3_{inj})$  relation is distinctly nonlinear, with  $S3_{VCSEL}$  peaking at  $\sim +/\sim -1$  for  $S3_{inj} \sim +/\sim -0.9$  and reducing thereafter. The VCSEL ellipticity is maximised when  $S3_{pump}$  is of the same sign as  $S3_{VCSEL}$ , but shows relatively little difference between  $S3_{pump}$  of  $+/\sim -0.25$  and  $+/\sim -1$ . This can be ascribed to the near-saturation of  $S3_{VCSEL}$  with  $S3_{pump}$  seen in figures 3,4 and in e.g. [4].

The position of the ellipticity peak, together with the general shape of the  $S3_{VCSEL}(S3_{inj})$  relation is seen to change with injection strength, shown in figure 8a,b, at linear pumping, and  $\gamma_{a,p^+}$  orientation. Separate signed  $\psi_{inj}$  (i.e.  $A, D$ ) for  $S3_{inj} -/+$  are used here, hence the discontinuity at  $S3_{inj} = 0$ . At linear injection,  $S3_{VCSEL}$  peaks at  $\kappa_{inj}/\kappa = 0.015$  and decreases with increasing injection ratio, in accordance with the results in figure 5 (green markers there).

Noting the reduced sensitivity of  $S3_{VCSEL}$  to  $\psi_{inj}$  with reduced birefringence in figure 6b, the SFM  $S3_{VCSEL}(S3_{inj})$  relation is shown with  $\gamma_p$  of  $0.2 \text{ ns}^{-1}$ , along with  $S3_{pump}$  of  $+0.25, 0.38$  in figure 9a,b respectively. The expected physical  $\gamma_s$  value of  $64 \text{ ns}^{-1}$  is again used. An arbitrary value of  $\psi_{inj}$  of  $+0.5$  (radians) is also used, due to the relative insensitivity of this parameter here. The solitary  $S3_{VCSEL}$ , without injection (black line), is now significantly higher than the figure 3 results due to the reduced birefringence, which is discussed in [4], [36], [39]. The shape of the  $S3_{VCSEL}(S3_{inj})$  relations and movement of the peak with  $\kappa_{inj}$  are similar to figure 8, except the  $S3_{VCSEL}$  values are much elevated (note the reduced plot ranges), and furthermore this result is not sensitive to  $\psi_{inj}$ .

## V. DISCUSSION AND FUTURE WORK

We have examined experimentally and theoretically the principal types of pump-VCSEL ellipticity response in the solitary QW spin-VCSEL, and how these depend on the relative signs of  $\alpha, \gamma_a$  and  $\gamma_p$ . Analysis of the linear polarisation angle  $\psi_{VCSEL}$  suggests that a negative sign of  $\alpha$  should be used in the current formulism of the SFM, in accordance with a recent report.



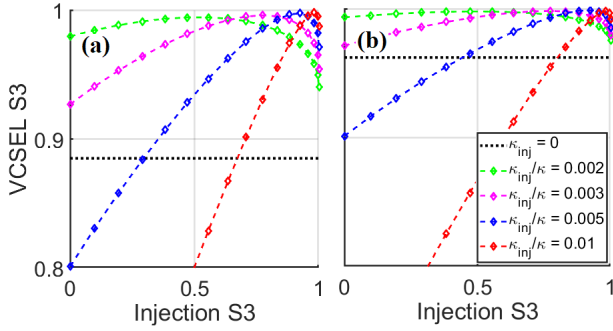


Fig. 9. SFM VCSEL  $S_3$  versus injection  $S_3$  with varying injection magnitude and reduced birefringence (a)  $\gamma_p = 0.2 \text{ ns}^{-1}$ ,  $S_{3 \text{ pump}} = 0.25$  (b)  $\gamma_p = 0.2 \text{ ns}^{-1}$ ,  $S_{3 \text{ pump}} = 0.38$ .

An analysis of the VCSEL ellipticity with linear and spin-polarised pumping and optical injection has found a dependence on the injection rate and birefringence. For linear pumping, steady state analysis of the SFM shows that a particular  $\kappa_{inj}/\kappa$  value (or correspondingly  $\tilde{E}_{inj}/\tilde{E}$ ) produces circular solutions for the injected VCSEL system. The results show also that finite birefringence shifts a sinusoidal VCSEL ellipticity peak towards the higher frequency axis, in accordance with results from the experiment and SFM.

The output-input ellipticity of the system shows unique nonlinear relationships. The parameters used in the SFM show that some of these responses can be tailored by changes in simple operational conditions e.g. relative injection strength, but others are reliant on selection of materials e.g. birefringence and spin relaxation rates. This suggests that with further exploitation of polarisation to encode data [13] these ellipticity properties might also be used, exploiting the unique spin coupling between electrons and photons in spin VCSELs. The varied ellipticity responses may have applications in logic operations and/or signal processing. For example, the approximately symmetrical peak for  $\kappa_{inj}/\kappa = 0.02$  (red line) in figure 8a may form the basis for an XOR gate with the right discrimination levels; the peaks skewed to higher  $S_{3 \text{ inj}}$  from higher injection coupling may form an AND or OR gate (e.g. blue lines figure 8a,b, red lines figure 9); and the peaks skewed towards zero  $S_{3 \text{ inj}}$  a NOR gate (black line figure 8a, red line figure 8b).

High values of the relative output to input ellipticity can be achieved under spin polarised pumping (figures 6, 9). This is similar to spin amplification of the pump, but requires much lower input power, demonstrating a potential application for regeneration of circularly polarised signals in future telecommunications systems. Furthermore, reduced birefringence (figure 6b, 9), which is feasible considering recent developments [35], [38]–[43] would give a very high output ellipticity for any input ellipticity or  $\psi_{inj}$ , creating a signal spin regenerator robust to the input polarisation state. Metamaterials [44]–[46], or other exotic materials such as chiral conjugated polymer films [47] have recently been investigated which can generate elliptic from linear polarisation. However, spin VCSELs also offer optical amplitude gain in addition to their polarisation responses. Such benefits are predicted for fairly modest spin-polarised

pumping ( $S_{3 \text{ pump}} = 0.25$  and  $0.38$  figure 9) and  $\gamma_s$  values consistent with current materials at room temperature. Values of this order may be achievable with spin-aligning electrical contacts [2], [48] for future applications.

## VI. CONCLUSIONS

We have demonstrated two types of pump-VCSEL polarisation response in a solitary spin VCSEL, depending on the magnitudes and signs of  $\alpha$ ,  $\gamma_a$  and  $\gamma_p$ . We have furthermore shown a range of output (VCSEL) versus input (optical injection) ellipticity responses depending on the injection magnitude and angle. Steady-state analysis based on the SFM for the case of linear pump and injection ellipticity supports the results. We have described how these novel output-input ellipticity responses, which can be tailored by choice of  $\gamma_p$ ,  $S_{3 \text{ pump}}$  and  $S_{3 \text{ inj}}$ , may be exploitable in logic or signal processing operations using only the ellipticity. High values of output ellipticity have been demonstrated for linear pumping under particular conditions, and more robustly with spin polarised pumping, with the former achievable in a non-spin laser, and the latter achievable with spin aligning electrical contacts or optical pumping.

## APPENDIX

### CONVERSION BETWEEN COMPLEX FIELD AND STOKES PARAMETERS

#### A. Stokes Parameters From Complex Linearly Polarized Fields

The Stokes parameters can be written in terms of the complex fields  $\tilde{E}_x = |\tilde{E}_x| \exp(i\phi_x)$ ,  $\tilde{E}_y = |\tilde{E}_y| \exp(i\phi_y)$  and phase difference  $\phi = \phi_y - \phi_x$  as [49]

$$S_1 = (|\tilde{E}_x|^2 - |\tilde{E}_y|^2) / (|\tilde{E}_x|^2 + |\tilde{E}_y|^2) \quad (\text{A1})$$

$$S_2 = 2|\tilde{E}_x||\tilde{E}_y| \cos \phi / (|\tilde{E}_x|^2 + |\tilde{E}_y|^2) \\ \equiv 2\text{Re}(\tilde{E}_x^* \tilde{E}_y) / (|\tilde{E}_x|^2 + |\tilde{E}_y|^2) \quad (\text{A2})$$

$$S_3 = -2|\tilde{E}_x||\tilde{E}_y| \sin \phi / (|\tilde{E}_x|^2 + |\tilde{E}_y|^2) \\ \equiv -2\text{Im}(\tilde{E}_x^* \tilde{E}_y) / (|\tilde{E}_x|^2 + |\tilde{E}_y|^2) \quad (\text{A3})$$

Note the change of sign for equation (A3) compared to equation (6.1-9d) in [48] due to the circular polarisation convention used (here  $\phi = -, +\pi/2$  for RCPLCP,  $\phi = +, -\pi/2$  for RCPLCP in [49]).

Using the Stokes parameters from (A1) – (A3),  $\psi$  can be generated using equation (5).

#### B. Complex Injection Fields From Stokes Parameters

We use a normalisation of the injection fields so that  $|\tilde{E}_{inj,x}|^2 + |\tilde{E}_{inj,y}|^2 = S_1^2 + S_2^2 + S_3^2 = 1$ . Firstly from (1) and (2),  $S_{1 \text{ inj}}, S_{2 \text{ inj}}$  are generated from  $S_{3 \text{ inj}}, \psi_{inj}$  as (A4), (A5), noting that  $-\pi \leq 2\psi_{inj} \leq \pi$  and  $-\pi/2 \leq 2\chi \leq \pi/2$ .

$$S_{1 \text{ inj}} = \sqrt{1 - S_{3 \text{ inj}}^2} \cos 2\psi_{inj} \quad (\text{A4})$$

$$S_{2 \text{ inj}} = \sqrt{1 - S_{3 \text{ inj}}^2} \sin 2\psi_{inj} \quad (\text{A5})$$



From (A1)

$$|\tilde{E}_{x,inj}| = \sqrt{(1 + S1_{inj})/2} \quad (A6)$$

$$|\tilde{E}_{y,inj}| = \sqrt{(1 - S1_{inj})/2} \quad (A7)$$

From (A2) and (A3) the phase difference  $\phi_{inj}$  can be derived as (A8), using the 4-quadrant atan2 function and noting that both  $S3_{inj}$  and  $S3_{inj}$  are signed values. Care is needed as (A8) is undefined for  $S2_{inj}$  of exactly zero, so  $\phi_{inj}$  cannot be derived for  $S2_{inj} = 0$  when both  $S1_{inj}$  and  $S3_{inj}$  are finite (if either  $S1_{inj}$  or  $S3_{inj}$  are unity,  $\phi_{inj}$  is directly apparent as  $\mathbb{Z}\pi$  or  $\mathbb{Z}\pi/2$ ). This also applies to other forms for  $\phi$  e.g. using (6.1-6)-(6.1.7) from [49], however,  $\phi_{inj}$  can be derived numerically in this situation.

$$\phi_{inj} = \tan^{-1} \left( -\frac{S3_{inj}}{S2_{inj}} \right) \quad (A8)$$

Noting that the Stokes parameters contain only the relative phase difference, there exists an infinite combination of absolute phases  $\phi_{y,inj}, \phi_{x,inj}$  that form a particular relative phase  $\phi_{inj} = \phi_{y,inj} - \phi_{x,inj}$ . To generate the complex injection fields, we choose the Jones vectors convention that the phase of  $\tilde{E}_{x,inj}$  is zero, therefore  $\tilde{E}_{x,inj} \equiv |\tilde{E}_{x,inj}|$ ,  $\tilde{E}_{y,inj} = |\tilde{E}_{y,inj}| \exp(i\phi_{inj})$ .

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